WELCOME

Chapter 16 Section 3: Inverse Functions Graphically \& Algebraically

## WARM-UP

- Graph: $f(x)=|x|-2$
- Evaluate the piecewise function:

$$
\begin{aligned}
f(x)= & x+2 \text { if } x \leq-2 \\
& -2 x-3 \text { if } x>-2
\end{aligned}
$$

$f(-3)=$
$f(5)=$

# Chap 16 Sect 3: Learning Targets 

- Write piecewise functions
- Understand what an inverse is, inverse of a function and what it represents.
- Find the inverse of a function Algebraically.
- Find the inverse using a graph.


## Writing Piecewise Functions

We can write a piecewise function by breaking the graph into intervals of constant change and finding their equation.


## Inverse

"Undoing," or working backwards to return to the original state or position is referred to as the inverse.

## Put in Box -> Close Box -> Wrap Box -> Give Box

Take out of Box <- Open Box <- Un-Wrap <- Take Box

## What is a Function? $f(x)$

A function is an operation on the $x$ inputs in the domain that creates the possible $f(x)$ outputs in the range.

$$
f(x)=-2 x+4
$$

$$
f(3)=
$$

$$
f(1)=
$$

Inputs/ Domain


Outputs/ Range


## Inverse Function $f^{-1}(x)$

Undoes original function, It takes the output of a function and does operations to arrive back at the original input.

$$
f(x)=-2 x+4 \quad f^{-1}(x)=\frac{x-4}{-2}
$$

Inputs/ Domain


Outputs/ Range


## Find the Inverse Algebraically

## Step 1:

$$
f(x)=-2 x+4
$$

Replace $f(x)$ with $y$.

## Step 2:

Switch the $x$ and $y$ variable
Step 3:
Solve for $\boldsymbol{y}$.
Step 4:
If $y$ function, replace $w / f^{-1}(x)$

## Find the Inverse Graphically

The graph of any function's inverse is the reflection of the original function over the line $y=x$

$$
f(x)=-2 x+4
$$


$f^{-1}(x)=\frac{x-4}{-2}$

